MARKING SCHEME

CLASS XII

MATHEMATICS (CODE-041)

SECTION: A (Solution of MCQs of 1 Mark each)

Q no.	ANS	HINTS/SOLUTION
1.	(D)	For a square matrix A of order $n \times n$, we have $A.(adj A) = A I_n$, where I_n is the identity matrix of order $n \times n$. So, $A.(adj A) = \begin{bmatrix} 2025 & 0 & 0 \\ 0 & 2025 & 0 \\ 0 & 0 & 2025 \end{bmatrix} = 2025I_3 \implies A = 2025 \& adj A = A ^{3-1} = (2025)^2$ $\therefore A + adj A = 2025 + (2025)^2$.
2.	(A)	$P \qquad Y \qquad W \qquad Y$ $\downarrow Order \qquad \downarrow Order \qquad \downarrow Order \qquad \downarrow Order$ $p \times k \qquad 3 \times k \qquad n \times 3 \qquad 3 \times k$ For PY to exist Order of WY $k = 3 \qquad = n \times k$ Order of PY = $p \times k$ For PY + WY to exist order (PY) = order (WY) $\therefore p = n$
3.	(C)	$y = e^{x} = \frac{dy}{dx} = e^{x}$ In the domain (R) of the function, $\frac{dy}{dx} > 0$, hence the function is strictly increasing in $(-\infty, \infty)$
4.	(B)	$ A = 5, B^{-1}AB ^2 = (B^{-1} A B)^2 = A ^2 = 5^2.$
5.	(B)	A differential equation of the form $\frac{dy}{dx} = f(x, y)$ is said to be homogeneous, if $f(x, y)$ is a homogeneous function of degree 0. Now, $x^n \frac{dy}{dx} = y \left(\log_e \frac{y}{x} + \log_e e \right) \Rightarrow \frac{dy}{dx} = \frac{y}{x^n} \left(\log_e e \cdot \left(\frac{y}{x} \right) \right) = f(x, y)$; (<i>Let</i>). $f(x, y)$ will be a homogeneous function of degree 0 , if $n = 1$.
6.	(A)	Method 1: (Short cut) When the points $(x_1, y_1), (x_2, y_2)$ and $(x_1 + x_2, y_1 + y_2)$ are collinear in the Cartesian plane then $\begin{vmatrix} x_1 - x_2 & y_1 - y_2 \\ x_1 - (x_1 + x_2) & y_1 - (y_1 + y_2) \end{vmatrix} = 0 \Rightarrow \begin{vmatrix} x_1 - x_2 & y_1 - y_2 \\ -x_2 & -y_2 \end{vmatrix} = (-x_1y_2 + x_2y_2 + x_2y_1 - x_2y_2) = 0$ $\Rightarrow x_2y_1 = x_1y_2.$

		Method 2:			
		When the points $(x_1, y_1), (x_2, y_2)$	x_{1}) and $(x_{1} + x_{2}, y_{1} + y_{2})$ are collinear in the Cartesian plane then		
		$\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_1 + x_2 & y_1 + y_2 & 1 \end{vmatrix} = 0$			
			$-1(x_1y_1+x_1y_2-x_1y_1-x_2y_1)+(x_1y_2-x_2y_1)=0$		
		$\Rightarrow x_2 y_1 = x_1 y_2.$			
7.	(A)	$A = \begin{bmatrix} 0 & 1 & c \\ -1 & a & -b \\ 2 & 3 & 0 \end{bmatrix}$			
			When the matrix A is skew symmetric then $A^T = -A \Rightarrow a_{ij} = -a_{ji}$;		
		\Rightarrow c = -2; a = 0 and b = 3			
		So, $a+b+c=0+3-2=1$.	So, $a+b+c=0+3-2=1$.		
8.	(C)	$P(\overline{A}) = \frac{1}{2}; P(\overline{B}) = \frac{2}{3}; P(A \cap B)$	$)=\frac{1}{4}$		
		$\Rightarrow P(A) = \frac{1}{2}; P(B) = \frac{1}{3}$			
		We have, $P(A \cup B) = P(A) + P(B) - P(A \cap B) = \frac{1}{2} + \frac{1}{3} - \frac{1}{4} = \frac{7}{12}$			
		$P\left(\frac{\overline{A}}{\overline{B}}\right) = \frac{P\left(\overline{A} \cap \overline{B}\right)}{P\left(\overline{B}\right)} = \frac{P\overline{(A \cup B)}}{P\left(\overline{B}\right)} = \frac{1 - P\left(A \cup B\right)}{P\left(\overline{B}\right)} = \frac{1 - \frac{7}{12}}{\frac{2}{3}} = \frac{5}{8}.$			
9.	(B)	For obtuse angle, $\cos \theta < 0 =>$	$\vec{p}.\vec{q} < 0$		
		$2\alpha^2-3\alpha+\alpha<0 \implies 2\alpha^2-2$	$2\alpha < 0 \Longrightarrow \alpha \in (0,1)$		
10.	(C)	$\left \vec{a} \right = 3, \left \vec{b} \right = 4, \left \vec{a} + \vec{b} \right = 5$			
		We have , $\left \vec{a} + \vec{b}\right ^2 + \left \vec{a} - \vec{b}\right ^2 = 2\left(\left \vec{a} - \vec{b}\right ^2\right)$	$\left \vec{a}\right ^2 + \left \vec{b}\right ^2 = 2(9+16) = 50 \Rightarrow \left \vec{a} - \vec{b}\right = 5.$		
11.	(B)	Corner point	Value of the objective function $Z = 4x + 3y$		
		1. O(0,0)	z = 0		
		2. <i>R</i> (40,0)	<i>z</i> = 160		
		3. Q(30,20)	z = 120 + 60 = 180		
		4. P(0,40)	<i>z</i> = 120		
		Since, the feasible region is bounded so the maximum value of the objective function $z = 180$ is at $Q(30, 20)$.			

20.	(A)	Both (A) and (R) are true and (R) is the correct explanation of (A).
19.	(A)	Both (A) and (R) are true and (R) is the correct explanation of (A).
		So, required area (in sq units) is $= \left 2 \int_{0}^{4} 2\sqrt{y} dy \right = 4 \left[\frac{y^{\frac{3}{2}}}{\frac{3}{2}} \right]_{0}^{4} = \frac{64}{3}.$
18.	(B)	continuous and differentiable at x = 2.5 .The required region is symmetric about the y - axis.
17.	(D)	The graph of the function $f: R \to R$ defined by $f(x) = [x]$; (where [.] denotes G.I.F) is a straight line $\forall x \in (2.5-h, 2.5+h)$, 'h' is an infinitesimally small positive quantity. Hence, the function is
		the minimum value of the objective function $Z = 18x + 10y$ is 134 at $P(3,8)$.
16.	(D)	Since the inequality $Z = 18x + 10y < 134$ has no point in common with the feasible region hence
15.	(B)	The graph represents $y = \cos^{-1} x$ whose domain is $[-1,1]$ and range is $[0,\pi]$.
		$y = x \log x - x + c$ hence the correct option is (B).
		$dy = \log x dx \implies \int dy = \int \log x dx$
14.	(B)	The given differential equation $e^{y'} = x \implies \frac{dy}{dx} = \log x$
		$\therefore \int_{0}^{2\pi} \csc^{7} x dx = 0; \text{ Using the property } \int_{0}^{2a} f(x) dx = 0, \text{ if } f(2a-x) = -f(x).$
		Now, $f(2\pi - x) = \csc^7(2\pi - x) = -\csc^7 x = -f(x)$
		Let $f(x) = \cos e c^7 x$.
13.	(A)	We know, $\int_{0}^{2a} f(x) dx = 0$, if $f(2a - x) = -f(x)$
		$= -\frac{1}{2}\sqrt{1 + \frac{1}{x^4}} + c = -\frac{1}{2x^2}\sqrt{1 + x^4} + c$
		$=-\frac{1}{4}\int \frac{dt}{t^{\frac{1}{2}}} = -\frac{1}{4} \times 2 \times \sqrt{t} + c$, where 'c' denotes any arbitrary constant of integration.
		(Let $1 + x^{-4} = 1 + \frac{1}{x^4} = t$, $dt = -4x^{-5}dx = -\frac{4}{x^5}dx \Rightarrow \frac{dx}{x^5} = -\frac{1}{4}dt$)
12.	(A)	$\int \frac{dx}{x^3 (1+x^4)^{\frac{1}{2}}} = \int \frac{dx}{x^5 \left(1+\frac{1}{x^4}\right)^{\frac{1}{2}}}$

Section –B

[This section comprises of solution of very short answer type questions (VSA) of 2 marks each]

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$\begin{vmatrix} z > 3x < 4 \\ z > x < -\frac{4}{3} \\ \therefore x \in \left(-\infty, -\frac{4}{3}\right) & 1 \end{vmatrix}$ 22. The marginal cost function is $C'(x) = 0.00039x^2 + 0.004x + 5.$ $C'(150) = \overline{1} 14.375.$ 1 23.(a) $y = \tan^{-1}x$ and $z = \log_{-}x$. Then $\frac{dy}{dx} = \frac{1}{1+x^2}$ $\frac{1}{2}$ and $\frac{dz}{dx} = \frac{1}{x}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{1}{2}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{1}{x}$ $\frac{1}{2}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{dy}{dz} = \frac{dy}{dz}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{dy}{dz} = (\cos x)^*. \text{ Then, } y = e^{z \log_{-} \cos x}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{dy}{dx} = (\cos x)^* (\log_{-} \cos x + x. \frac{1}{\cos(-\sin x)}) = \frac{dy}{dx} = e^{z \log_{-} \cos x} \frac{d}{dx} (x \log_{-} \cos x)$ $\frac{1}{2}$ $\frac{dy}{dx} = (\cos x)^* \left\{ \log_{-} \cos x + x. \frac{1}{\cos(-\sin x)} \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^* (\log_{-} \cos x - x \tan x).$ 1 24.(a) We have $\overline{b} + \lambda \overline{c} = (-1 + 3\lambda)i + (2 + \lambda) i + \overline{b}$ $(\overline{b} + \lambda \overline{c}) . \overline{a} = 0 \Rightarrow 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 = 0$ $\frac{1}{2}$ $\frac{1}{2}$	21	$\cot^{-1}(3x+5) > \frac{\pi}{4} = \cot^{-1}1$	$\frac{1}{2}$
$\begin{vmatrix} = x < -\frac{4}{3} \\ \therefore x \in \left(-\infty, -\frac{4}{3}\right) & 1 \end{vmatrix}$ 22. The marginal cost function is $C'(x) = 0.00039x^3 + 0.004x + 5.$ $C'(150) = \overline{1} 14.375.$ 1 23.(a) $y = \tan^{-1}x$ and $z = \log_{\tau}x$. Then $\frac{dy}{dx} = \frac{1}{1+x^2}$ $\begin{cases} \frac{dy}{dx} = \frac{1}{x} \\ \frac{dy}{dz} = \frac{dy}{dx} \\ \frac{dz}{dx} = \frac{1}{x} \\ \frac{1}{2} \\ \frac{dy}{dz} = \frac{dy}{dx} \\ \frac{dz}{dx} \\ \frac{dz}{dx} = \frac{1}{x} \\ \frac{1}{2} \\ \frac{dy}{dz} = \frac{dy}{dx} \\ \frac{dz}{dx} \\ \frac{dz}{dx} \\ \frac{dy}{dx} = (\cos x)^x. Then, y = e^{-\log_{x} \cos x} \\ 0 n differentiating both sides with respect to x, we get \frac{dy}{dx} = e^{-\log_{x} \cos x} \frac{d}{dx} (x \log_{x} \cos x) \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_{x} \cos x) \right\} \\ \frac{1}{2} \\ \frac{1}{2} \\ \frac{dy}{dx} = (\cos x)^x \left\{ \log_{x} \cos x \frac{d}{dx} (x) + 2(2 + \lambda) \right\} \\ \frac{1}{2} \\ $		=>3x + 5 < 1 (as cot ⁻¹ x is strictly decreasing function in its domain)	$\frac{1}{2}$
$\begin{array}{ c c c c c } & \therefore x \in \left(-\infty, -\frac{4}{3}\right) & 1 \\ \hline & 1 \\ \hline & 22. & \text{The marginal cost function is } C^*(x) = 0.00039x^2 + 0.004x + 5. & 1 \\ \hline & C^*(150) = ₹ 14.375. & 1 \\ \hline & C^*(150) = ₹ 14.375. & 1 \\ \hline & 1 \\ \hline & 23.(a) & y = \tan^{-1}x \text{ and } z = \log_e x. & & & & \\ \hline & & Then \frac{dy}{dx} = \frac{1}{1+x^2} & & & 1 \\ \hline & & & \frac{dy}{dx} = \frac{1}{x} & & & & 1 \\ \hline & & & \frac{dy}{dx} = \frac{dy}{dx} & & & \\ \hline & & & \frac{dy}{dx} = \frac{dy}{dx} & & & & \\ \hline & & & \frac{dy}{dx} = \frac{dy}{dx} & & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & \frac{1}{2} & & & \\ \hline & & & & & \frac{1}{2} & & \\ \hline & & & & & \frac{dy}{dx} = (\cos x)^*. & \text{Then, } y = e^{x \log_e \cos x} \\ \hline & & & & & & \frac{dy}{dx} = e^{x \log_e \cos x} \frac{d}{dx} (x \log_e \cos x) & & & \\ \hline & & & & & \frac{1}{2} & & \\ \hline & & & & & \frac{dy}{dx} = (\cos x)^* \left\{ \log_e \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_e \cos x) \right\} & & & & \frac{1}{2} \\ \hline & & & & & \frac{dy}{dx} = (\cos x)^* \left\{ \log_e \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_e \cos x) \right\} & & & & \frac{1}{2} \\ \hline & & & & & \frac{dy}{dx} = (\cos x)^* \left\{ \log_e \cos x + x \cdot \frac{1}{\cos x} (-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^* (\log_e \cos x - x \tan x) \\ 1 & & & & \frac{1}{2} \\ \hline & & & & & & \frac{1}{2} \\ \hline & & & & & & \frac{1}{2} \\ \hline & & & & & & \frac{1}{2} \\ \hline & & & & & & & \frac{1}{2} \\ \hline & & & & & & & & \frac{1}{2} \\ \hline & & & & & & & & \frac{1}{2} \\ \hline & & & & & & & & & & \frac{1}{2} \\ \hline & & & & & & & & & & & & \\ \hline & & & &$			
$\begin{array}{ c c c c c }\hline C'(150) = \overline{1} \ 14.375. & 1\\ \hline 23.(a) & y = \tan^{-1}x \ \text{and} \ z = \log_{e}x \\ \hline \text{Then} \ \frac{dy}{dx} = \frac{1}{1+x^{2}} & \frac{1}{2} \\ & \text{and} \ \frac{dx}{dx} = \frac{1}{x} & \frac{1}{2} \\ & \text{and} \ \frac{dx}{dx} = \frac{1}{x} & \frac{1}{2} \\ & \frac{dy}{dz} = \frac{dy}{dz} \\ & \text{So.} & \frac{1}{2} \\ & \text{So.} & \frac{1}{2} \\ & \frac{1}{2} \\ \hline \frac{1+x^{2}}{\frac{1}{x}} = \frac{x}{1+x^{2}}. & \frac{1}{2} \\ \hline \text{OR} & \text{Let } y = (\cos x)^{*}. \text{ Then, } y = e^{z\log_{e}\cos x} \\ & \text{On differentiating both sides with respect to } x, \text{ we get } \ \frac{dy}{dx} = e^{z\log_{e}\cos x} \frac{d}{dx}(x\log_{e}\cos x) & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e}\cos x) \right\} & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e}\cos x) \right\} & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x + x. \frac{1}{\cos x}(-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^{*} (\log_{e}\cos x - x\tan x). & 1 \\ \hline 24.(a) & \text{We have } \vec{b} + \lambda \vec{c} = (-1 + 3\lambda) \hat{1} + (2 + \lambda) \hat{1} + \hat{3} = 0 \\ & \lambda = -\frac{5}{a} \end{array}$			1
$\begin{array}{ c c c c c }\hline C'(150) = \overline{1} \ 14.375. & 1\\ \hline 23.(a) & y = \tan^{-1}x \ \text{and} \ z = \log_{e}x \\ \hline \text{Then} \ \frac{dy}{dx} = \frac{1}{1+x^{2}} & \frac{1}{2} \\ & \text{and} \ \frac{dx}{dx} = \frac{1}{x} & \frac{1}{2} \\ & \text{and} \ \frac{dx}{dx} = \frac{1}{x} & \frac{1}{2} \\ & \frac{dy}{dz} = \frac{dy}{dz} \\ & \text{So.} & \frac{1}{2} \\ & \text{So.} & \frac{1}{2} \\ & \frac{1}{2} \\ \hline \frac{1+x^{2}}{\frac{1}{x}} = \frac{x}{1+x^{2}}. & \frac{1}{2} \\ \hline \text{OR} & \text{Let } y = (\cos x)^{*}. \text{ Then, } y = e^{z\log_{e}\cos x} \\ & \text{On differentiating both sides with respect to } x, \text{ we get } \ \frac{dy}{dx} = e^{z\log_{e}\cos x} \frac{d}{dx}(x\log_{e}\cos x) & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e}\cos x) \right\} & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e}\cos x) \right\} & \frac{1}{2} \\ & \Rightarrow \frac{dy}{dx} = (\cos x)^{*} \left\{ \log_{e}\cos x + x. \frac{1}{\cos x}(-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^{*} (\log_{e}\cos x - x\tan x). & 1 \\ \hline 24.(a) & \text{We have } \vec{b} + \lambda \vec{c} = (-1 + 3\lambda) \hat{1} + (2 + \lambda) \hat{1} + \hat{3} = 0 \\ & \lambda = -\frac{5}{a} \end{array}$	22.	The marginal cost function is $C'(x) = 0.00039x^2 + 0.004x + 5$.	1
$\begin{array}{c} \begin{array}{c} \begin{array}{c} y \ \ \text{then } u \ \text{to } v \ \text{to } v$			1
$\begin{aligned} & \text{and } \frac{dz}{dx} = \frac{1}{x} \\ & \text{and } \frac{dz}{dx} = \frac{1}{x} \\ & \frac{dy}{dz} = \frac{dy}{dz} \\ & \frac{dz}{dx} \\ & \text{So,} \\ & = \frac{1}{\frac{1+x^2}{1}} = \frac{x}{1+x^2} \\ & \frac{1}{2} \end{aligned} \qquad $	23.(a)	$y = \tan^{-1} x$ and $z = \log_e x$.	
$\begin{vmatrix} \frac{dy}{dz} = \frac{\frac{dy}{dx}}{\frac{dz}{dx}} \\ \text{So,} & \frac{1}{\frac{1+x^2}{\frac{1}{x}}} = \frac{x}{1+x^2}, \\ \frac{1}{\frac{1}{x}} = \frac{1}{\frac{1+x^2}{\frac{1}{x}}} = \frac{x}{1+x^2}, \\ \frac{1}{\frac{1}{2}} & \frac{1}{\frac{1}{2}} \end{vmatrix}$ $Product OR = 1 \text{ Let } y = (\cos x)^x. \text{ Then, } y = e^{x\log_e \cos x} = \frac{1}{\frac{1}{2}} \text{ Cos } x^{-1} Co $		Then $\frac{dy}{dx} = \frac{1}{1+x^2}$	$\frac{1}{2}$
$\begin{aligned} \frac{1}{24.(a)} &= \frac{1}{1+x^2} = \frac{x}{1+x^2}, \\ \frac{1}{x} &= \frac{1}{1+x^2} = \frac{x}{1+x^2}, \\ \frac{1}{2} &= \frac{1}{x} = \frac{1}{x$			$\frac{1}{2}$
$\begin{aligned} \frac{1}{24.(a)} &= \frac{1}{1+x^2} = \frac{x}{1+x^2}, \\ \frac{1}{x} &= \frac{1}{1+x^2} = \frac{x}{1+x^2}, \\ \frac{1}{2} &= \frac{1}{x} = \frac{1}{x$		$\frac{dy}{dz} = \frac{\frac{dy}{dx}}{\frac{dz}{dz}}$	$\frac{1}{2}$
OR 23.(b)Let $y = (\cos x)^x$. Then, $y = e^{x \log_e \cos x}$ $\frac{dy}{dx} = e^{x \log_e \cos x} \frac{d}{dx} (x \log_e \cos x)$ $\frac{1}{2}$ On differentiating both sides with respect to x , we get $\frac{dy}{dx} = e^{x \log_e \cos x} \frac{d}{dx} (x \log_e \cos x)$ $\frac{1}{2}$ $\Rightarrow \frac{dy}{dx} = (\cos x)^x \left\{ \log_e \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_e \cos x) \right\}$ $\frac{1}{2}$ $\Rightarrow \frac{dy}{dx} = (\cos x)^x \left\{ \log_e \cos x + x \cdot \frac{1}{\cos x} (-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^x (\log_e \cos x - x \tan x) \cdot 1$ 124.(a)We have $\vec{b} + \lambda \vec{c} = (-1 + 3\lambda)\hat{i} + (2 + \lambda)\hat{j} + \hat{k}$ $\frac{1}{2}$ $(\vec{b} + \lambda \vec{c}) \cdot \vec{a} = 0 \Rightarrow 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 = 0$ 1 $\lambda = -\frac{5}{8}$ $\frac{1}{2}$		So, $\frac{dx}{1+x^2} = \frac{1}{1+x^2} = \frac{x}{1+x^2}$.	
On differentiating both sides with respect to x , we get $\frac{dy}{dx} = e^{x \log_e \cos x} \frac{d}{dx} (x \log_e \cos x)$ $\Rightarrow \frac{dy}{dx} = (\cos x)^x \left\{ \log_e \cos x \frac{d}{dx} (x) + x \frac{d}{dx} (\log_e \cos x) \right\}$ $\Rightarrow \frac{dy}{dx} = (\cos x)^x \left\{ \log_e \cos x + x \cdot \frac{1}{\cos x} (-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^x (\log_e \cos x - x \tan x) \cdot \frac{1}{2}$ $24.(a) \qquad \text{We have } \vec{b} + \lambda \vec{c} = (-1 + 3\lambda)\hat{i} + (2 + \lambda)\hat{j} + \hat{k}$ $(\vec{b} + \lambda \vec{c}) \cdot \vec{a} = 0 \Rightarrow 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 = 0$ $\frac{1}{2}$ $\frac{1}{2}$	OR		
$\Rightarrow \frac{dy}{dx} = (\cos x)^{x} \left\{ \log_{e} \cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e} \cos x) \right\} \qquad $	23.(b)	On differentiating both sides with respect to x , we get $\frac{dy}{dx} = e^{x \log_e \cos x} \frac{d}{dx} (x \log_e \cos x)$	$\frac{1}{2}$
24.(a) We have $\vec{b} + \lambda \vec{c} = (-1 + 3\lambda)\hat{i} + (2 + \lambda)\hat{j} + \hat{k}$ $(\vec{b} + \lambda \vec{c}) \cdot \vec{a} = 0 \implies 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 = 0$ $\lambda = -\frac{5}{8}$ OR		$\Rightarrow \frac{dy}{dx} = (\cos x)^{x} \left\{ \log_{e} \cos x \frac{d}{dx}(x) + x \frac{d}{dx}(\log_{e} \cos x) \right\}$	
$\vec{b} + \lambda \vec{c} \cdot \vec{a} = 0 \implies 2(-1+3\lambda) + 2(2+\lambda) + 3 = 0$ $\frac{1}{2}$ $\lambda = -\frac{5}{8}$		$\Rightarrow \frac{dy}{dx} = (\cos x)^x \left\{ \log_e \cos x + x \cdot \frac{1}{\cos x} (-\sin x) \right\} \Rightarrow \frac{dy}{dx} = (\cos x)^x (\log_e \cos x - x \tan x) \cdot \frac{1}{\cos x} (-\sin x) = 1 + \frac{1}{\cos x} ($	1
$(b + \lambda c) \cdot a = 0 \implies 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 \equiv 0$ $\frac{1}{2}$	24.(a)	We have $\vec{b} + \lambda \vec{c} = (-1 + 3\lambda)\hat{i} + (2 + \lambda)\hat{j} + \hat{k}$	$\frac{1}{2}$
$\Lambda = -\frac{1}{8}$		$(\vec{b} + \lambda \vec{c}) \cdot \vec{a} = 0 \implies 2(-1 + 3\lambda) + 2(2 + \lambda) + 3 = 0$	1
$\begin{array}{ c c c c c }\hline OR\\ 24.(b) & \overrightarrow{BA} = \overrightarrow{OA} - \overrightarrow{OB} = (4\hat{\imath} + 3\hat{k}) - \hat{k} = 4\hat{\imath} + 2\hat{k} & \hline \\ \hline 1\\ 2 & \hline $		$\lambda = -\frac{5}{8}$	$\frac{1}{2}$
		$\overrightarrow{BA} = \overrightarrow{OA} - \overrightarrow{OB} = (4\hat{\imath} + 3\hat{k}) - \hat{k} = 4\hat{\imath} + 2\hat{k}$	$\frac{1}{2}$



28(b)	Line perpendicular to the lines	
	$\vec{r} = 2\hat{i} + \hat{j} - 3\hat{k} + \lambda(\hat{i} + 2\hat{j} + 5\hat{k})$ and $\vec{r} = 3\hat{i} + 3\hat{j} - 7\hat{k} + \mu(3\hat{i} - 2\hat{j} + 5\hat{k})$.	
	has a vector parallel it is given by $\vec{b} = \vec{b_1} \times \vec{b_2} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 5 \\ 3 & -2 & 5 \end{vmatrix} = 20\hat{i} + 10\hat{j} - 8\hat{k}$	1
	$\therefore \text{ equation of line in vector form is } \vec{r} = -\hat{i} + 2\hat{j} + 7\hat{k} + a(10\hat{i} + 5\hat{j} - 4\hat{k})$	1
	And equation of line in cartesian form is $\frac{x+1}{10} = \frac{y-2}{5} = \frac{z-7}{-4}$	1
29. (a)	$\int \left\{ \frac{1}{\log_a x} - \frac{1}{(\log_a x)^2} \right\} dx$	
	$= \int \frac{dx}{\log_e x} - \int \frac{1}{(\log_e x)^2} dx = \frac{1}{\log_e x} \int dx - \int \left\{ \frac{d}{dx} \left(\frac{1}{\log_e x} \right) \int dx \right\} dx - \int \frac{1}{(\log_e x)^2} dx$	1
	$= \frac{x}{\log_e x} + \int \frac{1}{(\log_e x)^2} \frac{1}{x} \cdot x \cdot dx - \int \frac{1}{(\log_e x)^2} dx$	1
	$= \frac{x}{\log_e x} + \int \frac{1}{(\log_e x)^2} dx - \int \frac{dx}{(\log_e x)^2} = \frac{x}{\log_e x} + c;$	1
	where'c'is any arbitary constant of integration.	
OR 29.(b)	$\int_{0}^{1} x \left(1-x\right)^{n} dx$	
	$= \int_0^1 (1-x)\{1-(1-x)\}^n dx, \left(as, \int_0^a f(x)dx = \int_0^a f(a-x)dx\right)$	1
	$=\int_0^1 x^n (1-x) dx$	
	$=\int_{-\infty}^{1}x^{n}dx-\int_{-\infty}^{1}x^{n+1}dx$	$\frac{1}{2}$
	$= \int_{0}^{1} x^{n} dx - \int_{0}^{1} x^{n+1} dx$ $= \frac{1}{n+1} [x^{n+1}]_{0}^{1} - \frac{1}{n+2} [x^{n+2}]_{0}^{1}$	
		$\frac{1}{2}$
	$=\frac{1}{n+1} - \frac{1}{n+2} = \frac{1}{(n+1)(n+2)}.$	1
30.	The feasible region determined by the constraints, $2x + y \ge 3$, $x + 2y \ge 6$, $x \ge 0$, $y \ge 0$ is as shown.	





$$\Rightarrow k \left(1 + \frac{1}{5} + \frac{1}{5^2} + \frac{1}{5^3} + \dots \right) = 1$$

$$\Rightarrow k \left(\frac{1}{1 - \frac{1}{5}} \right) = 1 \Rightarrow k = \frac{4}{5}$$

So, $P(X < 3) = P(X = 0) + P(X = 1) + P(X = 2)$
$$= \frac{4}{5} \left(1 + \frac{1}{5} + \frac{1}{5^2} \right) = \frac{4}{5} \left(\frac{25 + 5 + 1}{25} \right) = \frac{124}{125}.$$

1
Section -D

[This section comprises of solution of long answer type questions (LA) of 5 marks each]

32.

$$y = 20\cos 2x; \left\{\frac{\pi}{6} \le x \le \frac{\pi}{3}\right\}$$

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$$\begin{array}{|c|c|c|c|} \hline 0, \frac{d}{dx} \left(\frac{dy}{dx} \right) \frac{dx}{dx} = \cos e \, e^2 \theta \\ \hline 0, \frac{d^2y}{dx^2} = -\frac{\csc^2 \theta}{c} \\ \hline \frac{d^2y}{dx^2} = \frac{c(1+\cot^2 \theta)^{\frac{3}{2}}}{-\csc^2 \theta} = \frac{-c(\cos e^{-\theta}\theta)^{\frac{3}{2}}}{\csc^{2\theta}\theta} = -C, \\ \hline \frac{1}{2} \\ \hline \frac{d^2y}{dx^2} = -\frac{c(\cos e^{-1}\theta)}{c} \\ \hline \frac{d^2y}{dx^2} = -\frac{c(\cos e^{-1}\theta)^{\frac{3}{2}}}{-\csc^2 \theta} = \frac{-c(\cos e^{-\theta}\theta)^{\frac{3}{2}}}{-\csc^{2\theta}\theta} = -C, \\ \hline \frac{1}{2} \\ \hline \frac{d^2y}{dx^2} = -\frac{c(\cos e^{-1}\theta)^{\frac{3}{2}}}{c} \\ \hline \frac{d^2y}{dx^2} = -\frac{c(\cos e^{-1}\theta)^{\frac{3}{2}}}{-\csc^2 \theta} = -C, \\ \hline \frac{1}{2} \\ \hline \frac{d^2y}{dx^2} = -\frac{c(-1)^2}{c} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2} \\ \hline \frac{d^2y}{dx^2} = -\frac{\csc^2 \theta}{c} \\ \hline \frac{d^2y}{dx^2} = -\frac{1}{c} \\ \hline \frac{d^2y}{dx^2} = -\frac{1}{c} \\ \hline \frac{d^2y}{dx^2} = -\frac{1}{c} \\ \hline \frac{1}{2} \\ \hline \frac{1}{c} \\ \hline \frac$$

$$\frac{\&(\mu - 7\lambda + 4), 1 + (-2\mu + 6\lambda + 6), (-2) + (\mu - \lambda + 8), 1 = 0}{\Rightarrow 20\mu - 86\lambda = 0 \Rightarrow 10\mu - 43\lambda = 0.86\mu - 20\lambda = 0 \Rightarrow 3\mu - 10\lambda = 0}$$
In solving the above equations, we get $\mu = \lambda = 0$
So, the position vector of the points *P* and *Q* are $-i - j - k$ and $3i + 5j + 7k$ respectively.

$$\frac{PQ}{PQ} = 4i + 6j + 8k$$
 and

$$\frac{PQ}{PQ} = \sqrt{4^2 + 6^2 + 8^2} = \sqrt{116} = 2\sqrt{29}$$
 units.
In
OR
35.(b)

$$\frac{P(1,24)}{A}$$
Let $P(1, 2, 1)$ be the given point and *L* be the foot of the perpendicular from *P* to the given line *AB*
(*as shown* in *the figure above*).
Let's put $\frac{T-3}{1} = \frac{y+1}{2} = \frac{z-3}{-1} = \lambda$. Then, $x = \lambda + 3, y = 2\lambda - 1, z = 3\lambda + 1$
Let the coordinates of the point *L* be $(\lambda + 3, 2\lambda - 1, 3\lambda + 1)$.
So, direction ratios of *PL* are $(\lambda + 3 - 1, 2\lambda - 1 - 2, 3\lambda + 1 - 1)i.e., (\lambda + 2, 2\lambda - 3, 3\lambda)$
Direction ratios of the given line are $1, 2$ and 3 , which is perpendicular to *PL*. Therefore, we have,
 $(\lambda + 2), 1 + (2\lambda - 3), 2 + 3\lambda, 3 = 0 \Rightarrow 14\lambda = 4 \Rightarrow \lambda = \frac{2}{7}$
Then, $\lambda + 3 = \frac{2}{7} + 3 = \frac{37}{7}; 2\lambda - 1 = 2(\frac{2}{7}) - 1 = -\frac{3}{7}; 3\lambda + 1 = 3(\frac{2}{7}) + 1 = \frac{13}{7}$
Therefore, condinates of the point *L* are $(\frac{23}{7}, -\frac{7}{7}, \frac{12}{7})$.
Let $Q(x_1, y_1, z_1)$ be the image of $P(1, 2, 1)$ with respect to the given line. Then, *L* is the mid-point of *PQ*.
Therefore, $\frac{14x_4}{z} = \frac{23}{7}, \frac{14x_4}{z} = \frac{-3}{7}, \frac{14x_3}{z} = \frac{53}{7}, y_1 = -\frac{20}{7}, \frac{20}{7}, \frac{19}{7}$).
Let quation of the line joining $P(1, 2, 1)$ and $Q(\frac{59}{7}, -\frac{20}{7}, \frac{7}{7})$ is

x-1 $y-2$ $z-1$ $x-1$ $y-2$ $z-1$	1
$\frac{32}{7} - \frac{-34}{7} - \frac{12}{12} - \frac{7}{16} - \frac{-17}{-17} - \frac{-6}{6}$	

Section –E

[This section comprises solution of 3 case- study/passage based questions of 4 marks each with two sub parts. Solution of the first two case study questions have three sub parts (i),(ii),(iii) of marks 1,1,2 respectively. Solution of the third case study question has two sub parts of 2 marks each.)

36.	(i) $V = (40 - 2x)(25 - 2x)xcm^3$	1
	(ii) $\frac{dV}{dx} = 4(3x - 50)(x - 5)$	1
	(iii) (a) For extreme values $\frac{dV}{dx} = 4(3x - 50)(x - 5) = 0$	¹ / ₂
	$\Rightarrow x = \frac{50}{3} \text{ or } x = 5$	¹ / ₂
	$\frac{d^2V}{dx^2} = 24x - 260$	¹ / ₂
	$\therefore \frac{d^2 V}{dx^2} \text{ at } x = 5 \text{ is} - 140 < 0$	¹ / ₂
	$\therefore V \text{ is max } when x = 5$	
	(iii) OR	1.
	(b) For extreme values $\frac{dV}{dx} = 4(3x^2 - 65x + 250)$	¹ / ₂
	$\frac{d^2 V}{dx^2} = 4(6x - 65)$	¹ / ₂
	$\frac{dV}{dx} at x = \frac{65}{6} \text{ exists and } \frac{d^2V}{dx^2} at x = \frac{65}{6} is 0.$	
	$\frac{d^2V}{dx^2}$ at $x = \left(\frac{65}{6}\right)^-$ is negative and $\frac{d^2V}{dx^2}$ at $x = \left(\frac{65}{6}\right)^+$ is positive	¹ / ₂
	$\therefore x = \frac{65}{6}$ is a point of inflection.	¹ / ₂
37.	(i) Number of relations is equal to the number of subsets of the set $B \times G = 2^{n(B \times G)}$ = $2^{n(B) \times n(G)} = 2^{3 \times 2} = 2^{6}$	1
	(Wheren(A) denotes the number of the elements in the finite set A)	
		1
	(iii) (a) (A) reflexive but not symmetric = $\{(b_1, b_2), (b_2, b_1), (b_1, b_1), (b_2, b_2), (b_3, b_3), (b_2, b_3)\}.$	
	$((v_1, v_2), (v_2, v_1), (v_1, v_1), (v_2, v_2), (v_3, v_3), (v_2, v_3)).$	

	So the minimum number of elements to be added are	
	$(b_1, b_1), (b_2, b_2), (b_3, b_3), (b_2, b_3)$	1
	{Note : it can be any one of the pair from, $(\boldsymbol{b}_3, \boldsymbol{b}_2)$, $(\boldsymbol{b}_1, \boldsymbol{b}_3)$, $(\boldsymbol{b}_3, \boldsymbol{b}_1)$ in place of	
	(b ₂ , b ₃) also}	
	(B) reflexive and symmetric but not transitive =	
	$\{(b_1, b_2), (b_2, b_1), (b_1, b_1), (b_2, b_2), (b_3, b_3), (b_2, b_3), (b_3, b_2) \}.$	
	So the minimum number of elements to be added are	1
	$(b_1, b_1), (b_2, b_2), (b_3, b_3), (b_2, b_3), (b_3, b_2)$	
	OR (iii) (b) One-one and onto function	
	$x^2 = 4y. \operatorname{let} y = f(x) = \frac{x^2}{4}$	
	Let $x_1, x_2 \in [0, 20\sqrt{2}]$ such that $f(x_1) = f(x_2) \Rightarrow \frac{{x_1}^2}{4} = \frac{{x_1}^2}{4}$	1
	$\Rightarrow x_1^2 = x_2^2 \Rightarrow (x_1 - x_2)(x_1 + x_2) = 0 \Rightarrow x_1 = x_2 \text{ as } x_1, x_2 \in [0, 20\sqrt{2}]$	
	f is one-one function Now, $0 \le y \le 200$ hence the value of y is non-negative	
	and $f(2\sqrt{y}) = y$	
	\therefore for any arbitrary $y \in [0, 200]$, the pre-image of y exists in $[0, 20\sqrt{2}]$	1
	hence <i>f</i> is onto function.	
38.	Let E_1 be the event that one parrot and one owl flew from cage $-I$	
	E_2 be the event that two parrots flew from Cage-I	
	A be the event that the owl is still in cage-I	
	(i) Total ways for A to happen	
	From cage I 1 parrot and 1 owl flew and then from Cage-II 1 parrot and 1 owl	
	flew back + From cage I 1 parrot and 1 owl flew and then from Cage-II 2 parrots	
	flew back + From cage I 2 parrots flew and then from Cage-II 2 parrots came	1
	back.	$\frac{1}{2}$
	$= (5_{C_1} \times 1_{C_1})(7_{C_1} \times 1_{C_1}) + (5_{C_1} \times 1_{C_1})(7_{C_2}) + (5_{C_2})(8_{C_2})$	
	Probability that the owl is still in cage $-I = P(E_1 \cap A) + P(E_2 \cap A)$	
	$\frac{(5_{C_1} \times 1_{C_1})(7_{C_1} \times 1_{C_1}) + (5_{C_2})(8_{C_2})}{(5_{C_1} \times 1_{C_1})(7_{C_1} \times 1_{C_1}) + (5_{C_1} \times 1_{C_1})(7_{C_2}) + (5_{C_2})(8_{C_2})}$	1
		1
	$=\frac{35+280}{35+105+280}=\frac{315}{420}=\frac{3}{4}$	$\frac{1}{2}$

(i) The probability that one parrot and the owl flew from Cage-I to Cage-II given
that the owl is still in cage-I is
$$P\left(\frac{E_1}{A}\right)$$

 $P\left(\frac{E_1}{A}\right) = \frac{P(E_1 \cap A)}{P(E_1 \cap A) + P(E_2 \cap A)}$ (by Baye's Theorem)
 $= \frac{\frac{35}{420}}{\frac{315}{420}} = \frac{1}{9}$ 1